AI504: Programming for Artificial Intelligence

Week 10: Recurrent Neural Network

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Today’s Topic

- Recurrent Neural Network
  - Vanilla RNN
  - Bidirectional RNN
  - GRU, LSTM
- Sequence-to-sequence
  - Neural Machine Translation
- Attention

Recurrent Neural Network

Handling Variable-Length Sequences

- Image-to-Label

  VS

- Sentence-to-Label

Handling Variable-Length Sequences

- Image-to-Label ➔ Input size is fixed

  VS

- Sentence-to-Label ➔ Input size varies by sample

Bag-of-Words

- Classical way to handle variable length sentences/documents
- I gave the ball to John, who gave it to Mary
  - I:1, gave:2, the:1, ball:1, to:2, John:1, who:1, it:1, Mary:1

Bag-of-Words

- I gave the ball to John, who gave it to Mary
  - I:1, gave:2, the:1, ball:1, to:2, John:1, who:1, it:1, Mary:1

All vocab	Word count
a	0
aardvark	0
ab	0
…	…
…	…
ball	2
…	…
gave	2
…	…

Bag-of-Words

- I gave the ball to John, who gave it to Mary
  - I:1, gave:2, the:1, ball:1, to:2, John:1, who:1, it:1, Mary:1
- I gave the ball to Mary, who gave it to John
  - I:1, gave:2, the:1, ball:1, to:2, John:1, who:1, it:1, Mary:1

- Different meaning, same representation!

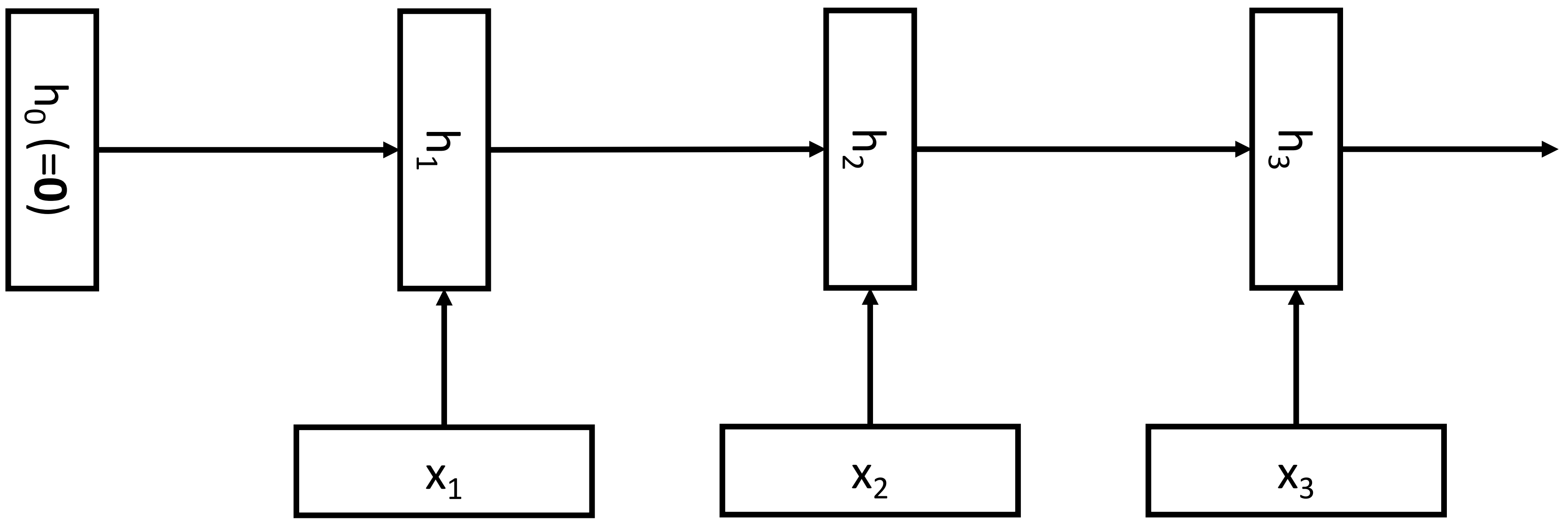
Classical NLP

- Syntax, Semantic, Discourse, Pragmatic
- Part-of-speech tagging
- Parsing
- Named entity recognition
- Semantic role labeling

- Many of them made obsolete by deep learning
- Or are they…?

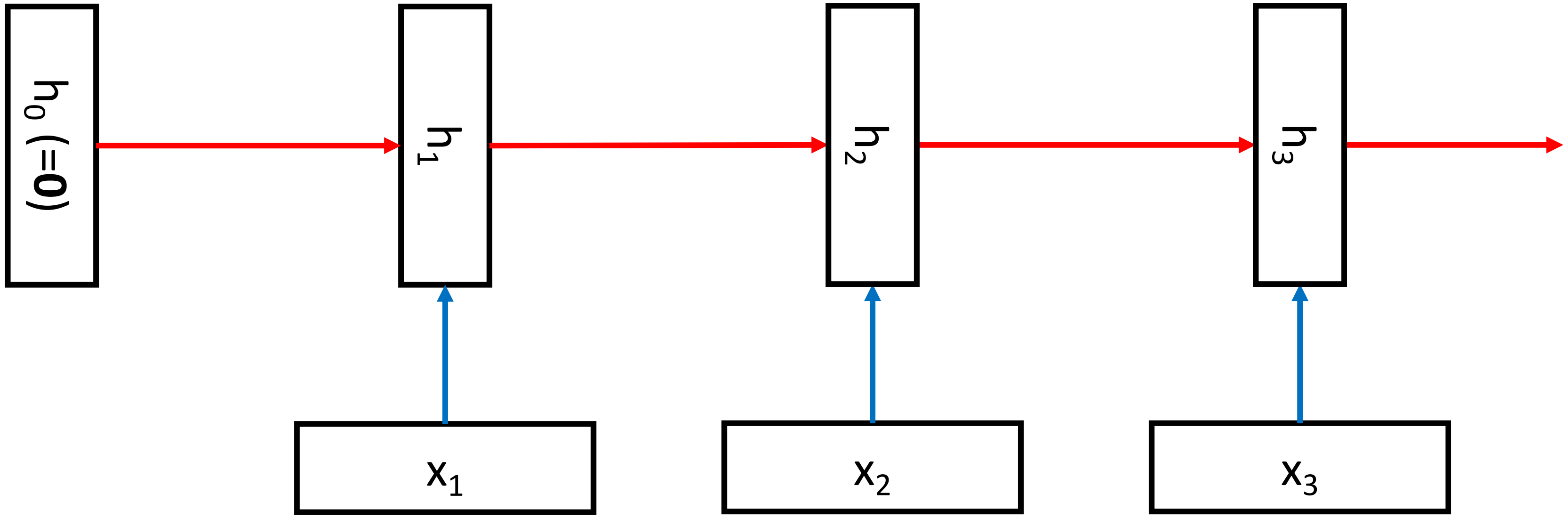
Recurrent Neural Network

- Represent variable-length input
- $\mathbf{h}_t = f(W\mathbf{x}_t + U\mathbf{h}_{t-1} + \mathbf{b})$
  - f: non-linear activation function (originally tanh)



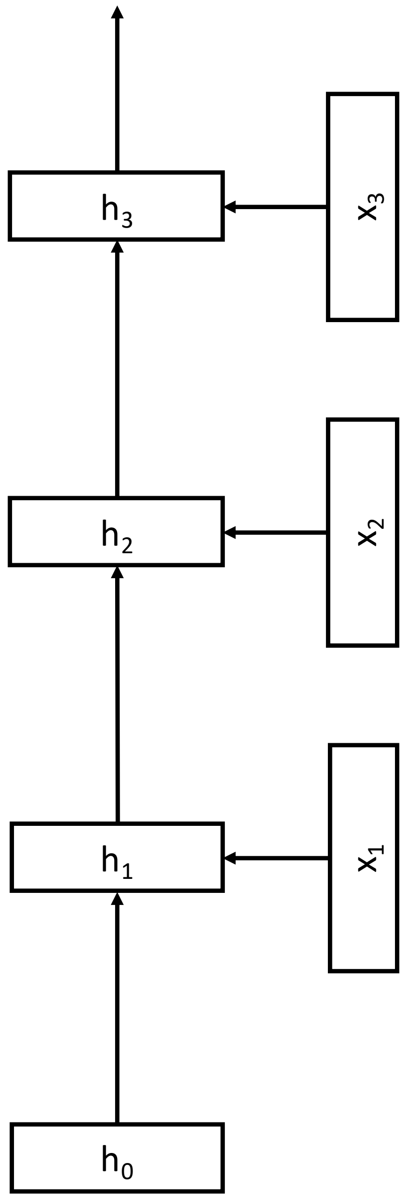
RNN

- Represent variable-length input
- Same weights at each timestep to handle variable-length sequence
  - U: h_{t-1} to h_t
  - W: x_t to h_t



RNN

- Represent variable-length input
- Feedforward Neural Network with new information at each timestep.
  - But use the same weights repeatedly.



Application

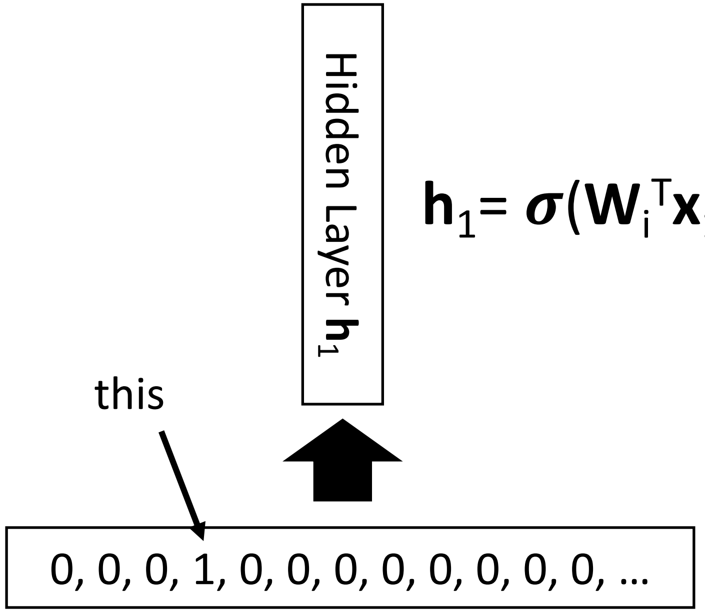
- Sequence-level classification/regression
  - Sentiment classification
  - Topic classification
- Classification/regression at each step.
  - Language modeling
  - Part-of-speech tagging
- Sequence-to-sequence
  - Translation
  - Question answering

Sequence-level Classification

- Sentiment classification: Positive or Negative?
  - “This movie is as impressive as a preschool Christmas play”

Sequence prediction with RNN

- Sentiment classification: Positive or Negative?
  - “This movie is as impressive as a preschool Christmas play”

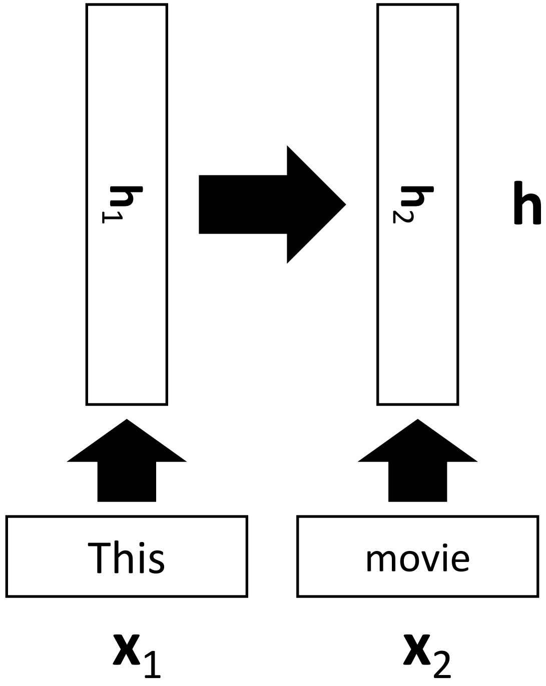


$\mathbf{h}_1 = \boldsymbol{\sigma}(\mathbf{W}_i^{T}\mathbf{x}_1)$

$\mathbf{x}_1$ (a vector with 1M elements. Only “this” is 1.)

Sequence prediction with RNN

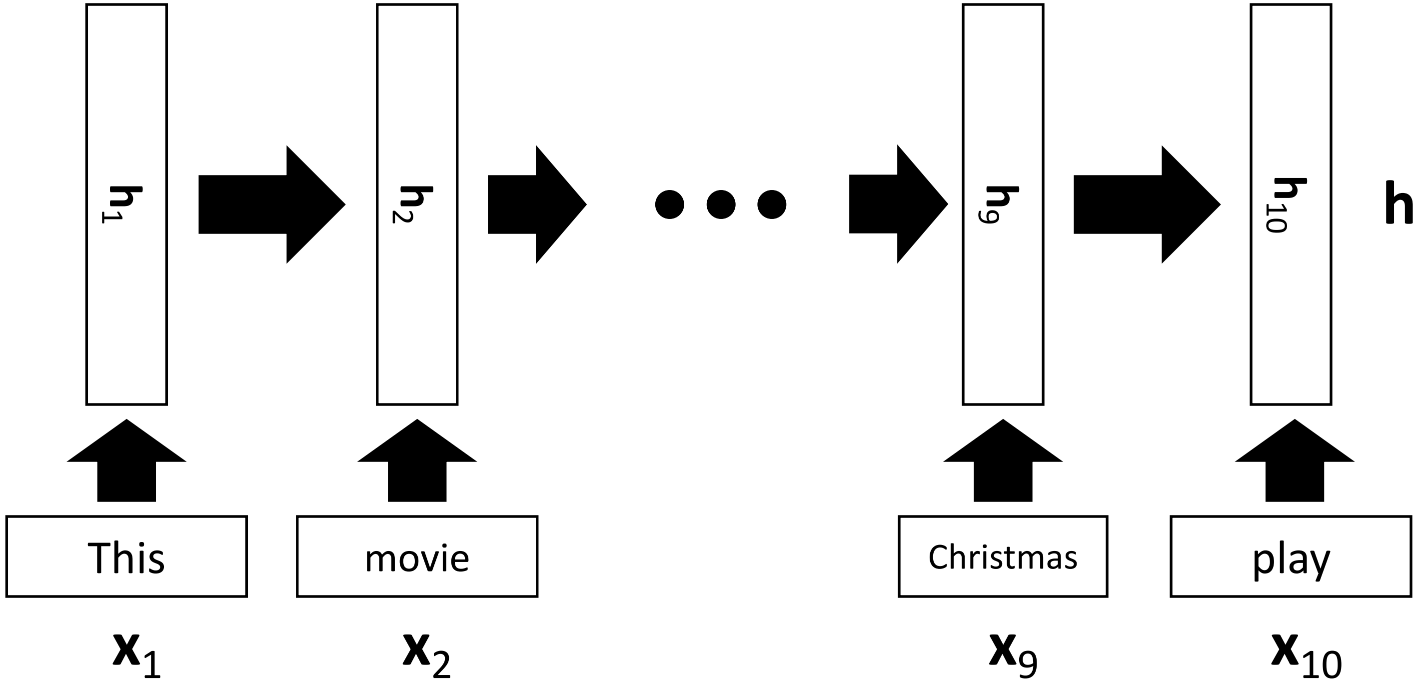
- Sentiment classification: Positive or Negative?
  - “This movie is as impressive as a preschool Christmas play”



$$\mathbf{h}_2 = \sigma(\mathbf{W}_h^T \mathbf{h}_1 + \mathbf{W}_i^T \mathbf{x}_2)$$

Sequence prediction with RNN

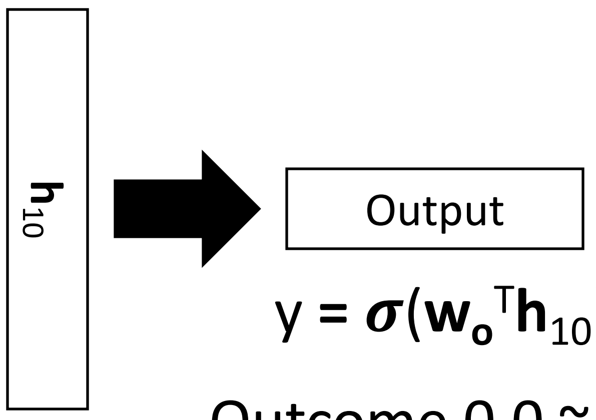
- Sentiment classification: Positive or Negative?
  - “This movie is as impressive as a preschool Christmas play”



$$\mathbf{h}_{10} = \sigma(\mathbf{W}_h^T \mathbf{h}_9 + \mathbf{W}_i^T \mathbf{x}_{10})$$

Sequence prediction with RNN

- Sentiment classification: Positive or Negative?
  - "This movie is as impressive as a preschool Christmas play"



$y = \boldsymbol{\sigma}(\mathbf{w_o}^T \mathbf{h}_{10})$

Outcome 0.0 ~ 1.0

Language Modeling

- p("This movie is as impressive as a preschool Christmas play")
  - What is the probability of this sentence?
  - (Probably super small…)

Language Modeling

- p("This movie is as impressive as a preschool Christmas play")

$\Downarrow$

- p(This)*p(movie | This)*p(is | This, movie)*…*p(play | This, movie, …, Christmas)

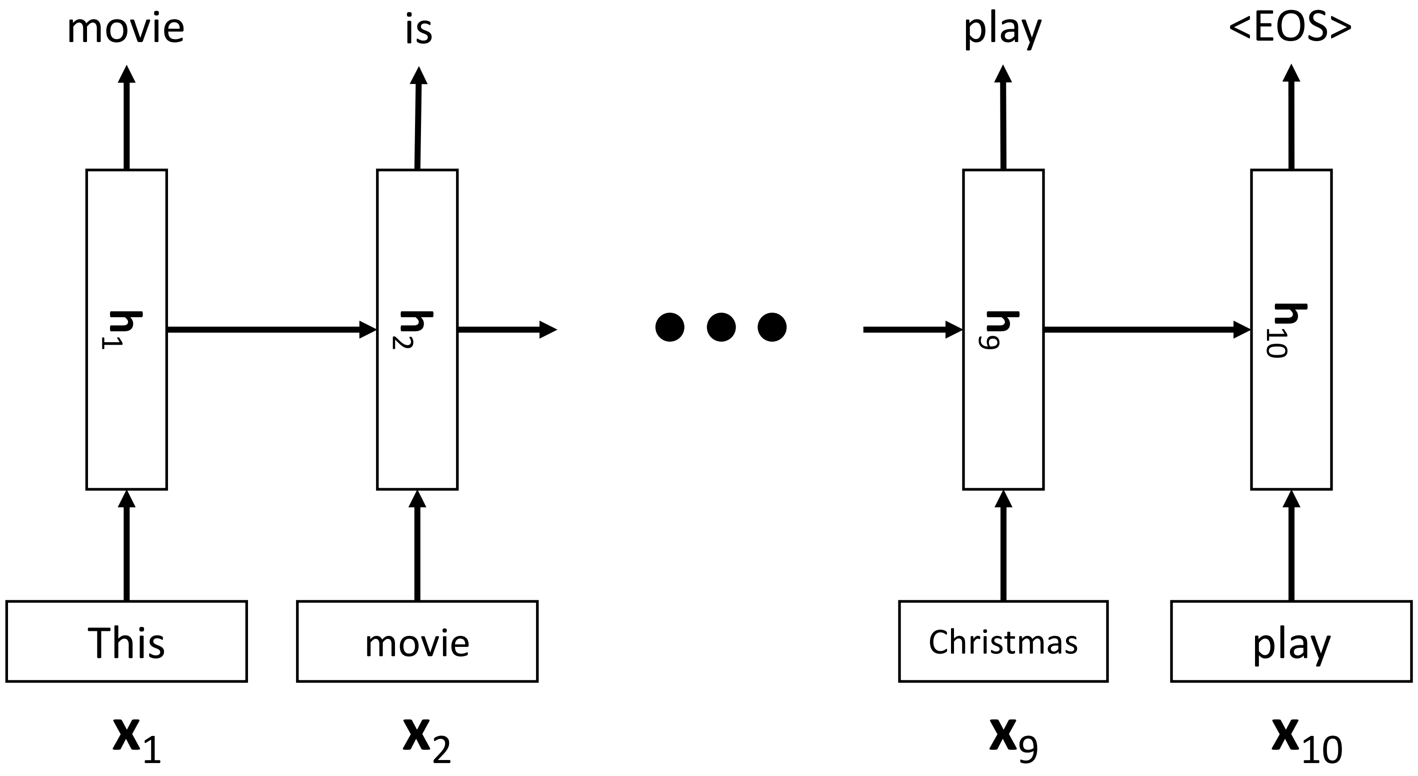
- Need a model that can perform:
  - $p(w_t \mid w_1, w_2, \ldots w_{t-1})$

Language Modeling

- p("This movie is as impressive as a preschool Christmas play")
  - p(This)*p(movie | This)*p(is | This, movie)*…*p(play | This, movie, …, Christmas)
- Need a model that can perform:
  - $p(w_t \mid w_1, w_2, \dots w_{t-1})$
- Traditionally:
  - Unigram, bigram, trigram
  - Bigram ➔ $p(w_t \mid w_{t-1})$, Trigram ➔ $p(w_t \mid w_{t-2}, w_{t-1})$
  - Limited horizon
- With RNN
  - Theoretically, can model full $p(w_t \mid w_1, w_2, \dots w_{t-1})$

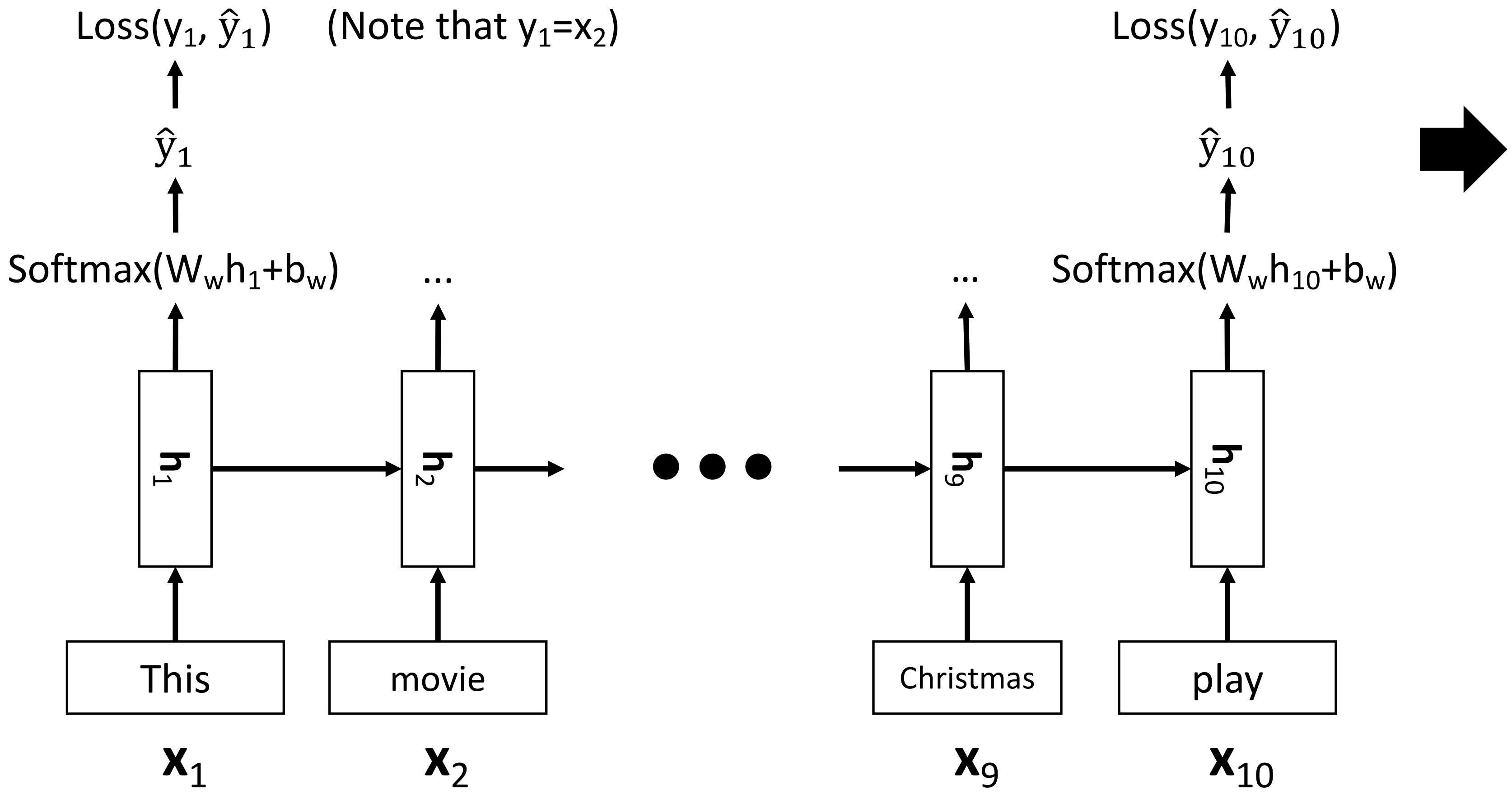
Language Modeling with RNN

- “This movie is as impressive as a preschool Christmas play”



Language Modeling with RNN

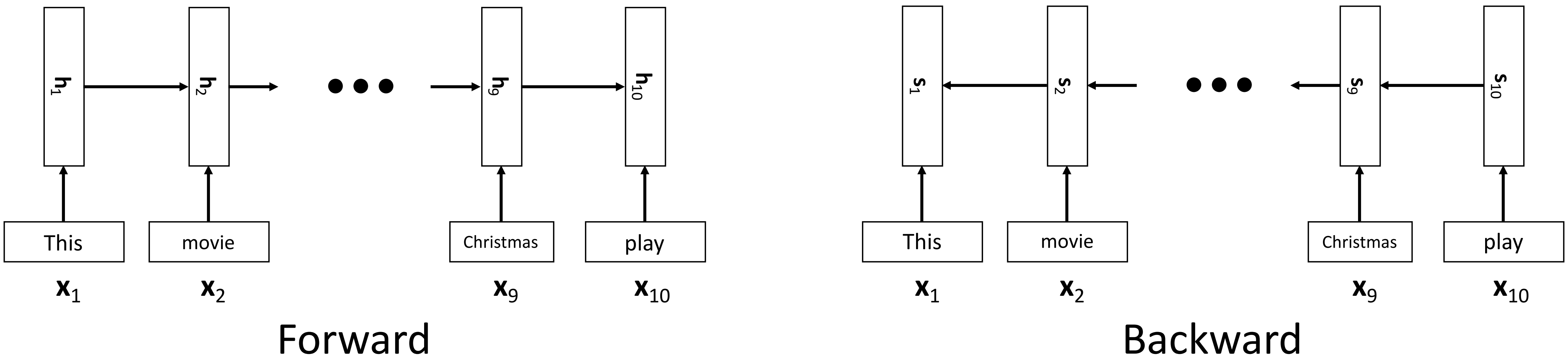
- "This movie is as impressive as a preschool Christmas play"



10 loss terms for
a single sentence
(Loss is usually
negative log-likelihood)

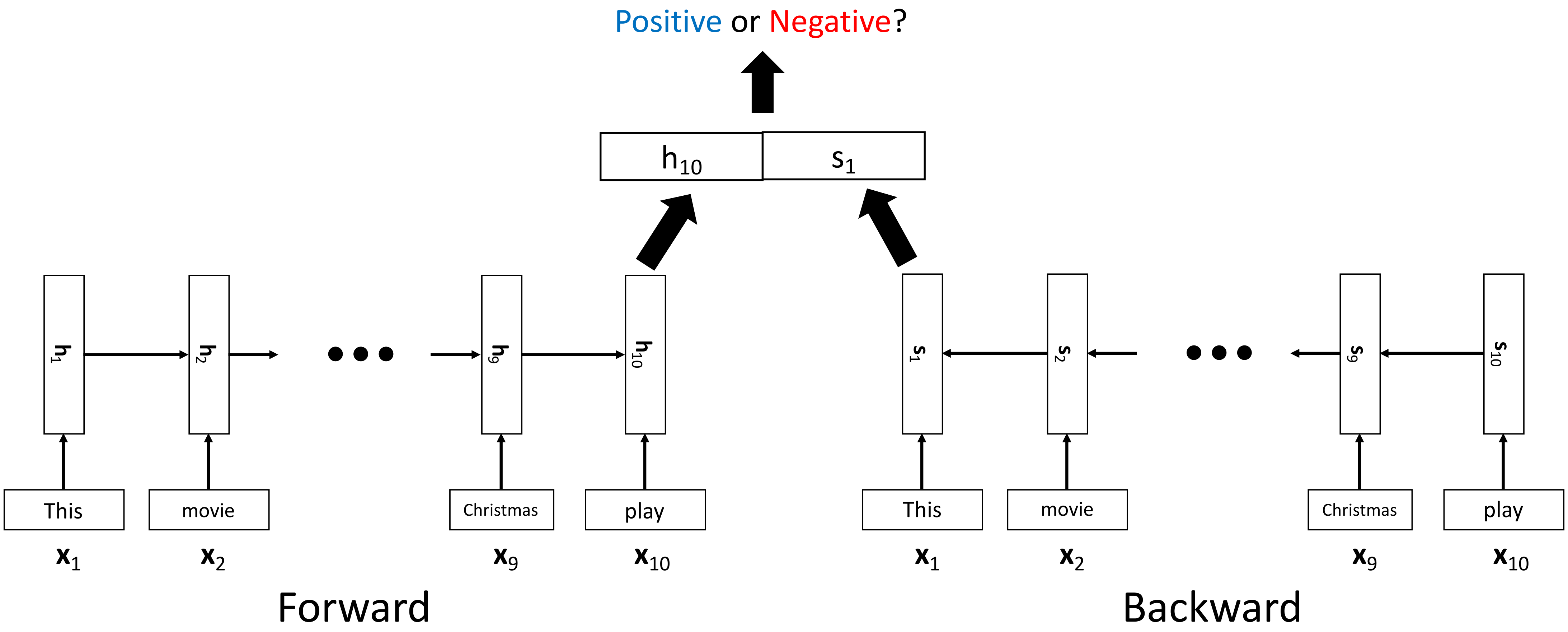
Bidirectional RNN

- Encode a sequence in two directions



Bidirectional RNN

- Encode a sequence in two directions



Limitation

- Vanishing gradient still exists.
  - Long sequence means long backpropagation chain!
- Input from a distant past is forgotten!
  - Ex: “Jane walked into the room. John walked in too. It was late in the day. Jane said hi to ____ ”
- How to remedy this?
  - Some old tricks: Initialize weight matrices to identity matrices, use ReLU.
- Exploding gradient also exists.
  - Popular remedy: gradient clipping

Gated Recurrent Unit

- More complex hidden unit computation in recurrence!
- Gated Recurrent Units (GRU) introduced by Cho et al. 2014 (see reading list)
- Main ideas:
  - keep around memories to capture long distance dependencies
  - allow error messages to flow at different strengths depending on the inputs

Reference: https://cs224d.stanford.edu/lectures/CS224d-Lecture9.pdf

Gated Recurrent Unit

- Standard RNN computes hidden layer at next time step directly: $h_t = f\left(W^{(hh)}h_{t-1} + W^{(hx)}x_t\right)$
- GRU first computes an update **gate** (another layer) based on current input word vector and hidden state

$$z_t = \sigma\left(W^{(z)}x_t + U^{(z)}h_{t-1}\right)$$

- Compute reset gate similarly but with different weights

$$r_t = \sigma\left(W^{(r)}x_t + U^{(r)}h_{t-1}\right)$$

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Gated Recurrent Unit

- Update gate $$z_t = \sigma\left(W^{(z)}x_t + U^{(z)}h_{t-1}\right)$$
- Reset gate $$r_t = \sigma\left(W^{(r)}x_t + U^{(r)}h_{t-1}\right)$$
- New memory content: $$\tilde{h}_t = \tanh\left(Wx_t + r_t \circ Uh_{t-1}\right)$$
  If reset gate unit is ~0, then this ignores previous memory and only stores the new word information
- Final memory at time step combines current and previous time steps: $$h_t = z_t \circ h_{t-1} + (1 - z_t) \circ \tilde{h}_t$$

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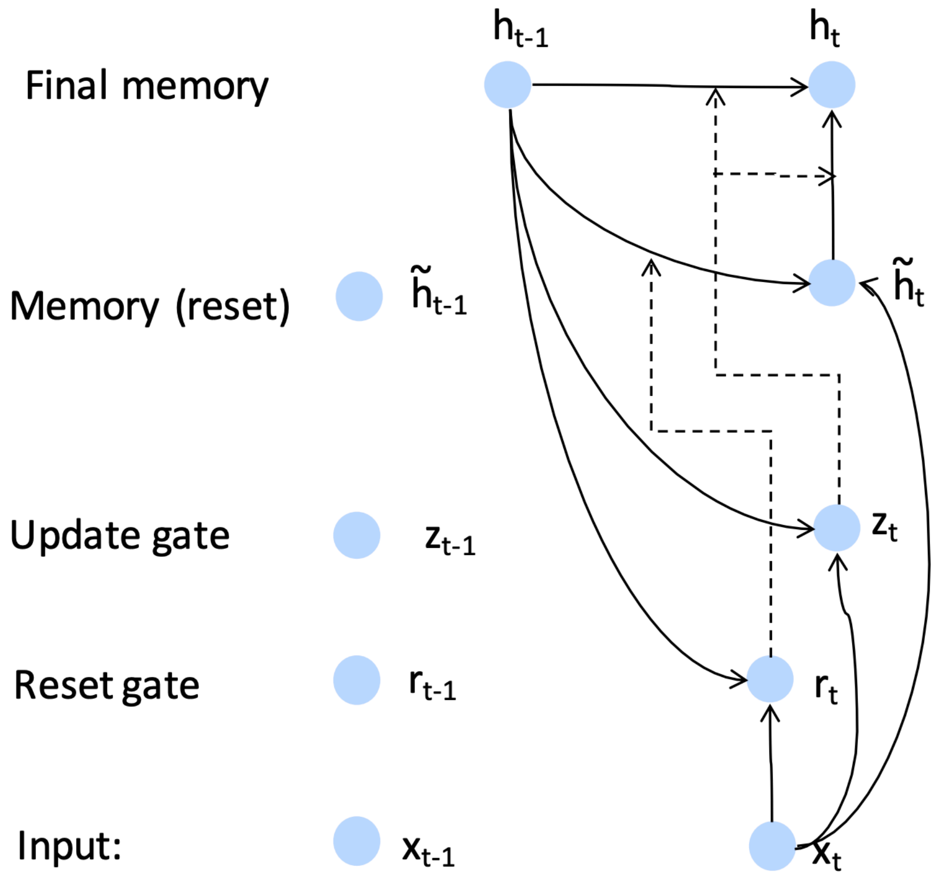
Gated Recurrent Unit



$$z_t = \sigma\left(W^{(z)}x_t + U^{(z)}h_{t-1}\right)$$
$$r_t = \sigma\left(W^{(r)}x_t + U^{(r)}h_{t-1}\right)$$
$$\tilde{h}_t = \tanh\left(Wx_t + r_t \circ Uh_{t-1}\right)$$
$$h_t = z_t \circ h_{t-1} + (1 - z_t) \circ \tilde{h}_t$$

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Long Short Term Memory

- We can make the units even more complex
- Allow each time step to modify
  - Input gate (current cell matters) $i_t = \sigma\left(W^{(i)}x_t + U^{(i)}h_{t-1}\right)$
  - Forget (gate 0, forget past) $f_t = \sigma\left(W^{(f)}x_t + U^{(f)}h_{t-1}\right)$
  - Output (how much cell is exposed) $o_t = \sigma\left(W^{(o)}x_t + U^{(o)}h_{t-1}\right)$
  - New memory cell $\tilde{c}_t = \tanh\left(W^{(c)}x_t + U^{(c)}h_{t-1}\right)$
- Final memory cell: $c_t = f_t \circ c_{t-1} + i_t \circ \tilde{c}_t$
- Final hidden state: $h_t = o_t \circ \tanh(c_t)$

Reference: https://cs224d.stanford.edu/lectures/CS224d-Lecture9.pdf

Sequence-to-Sequence

Sequence-to-Sequence

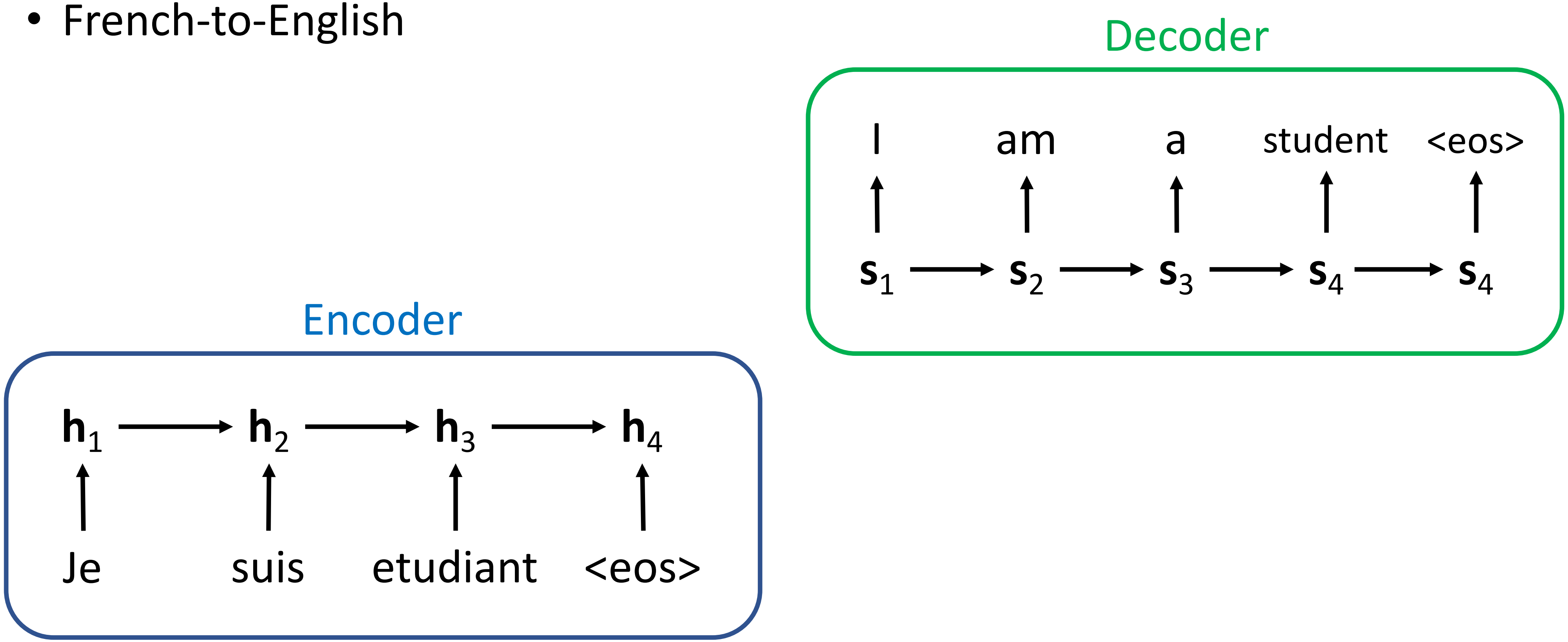
- Given variable-length sequence input,

  Predict (Generate) variable-length sequence output
  - Machine translation
  - Question answering
  - Chatbot

- Naturally, we need two RNNs!
  - Why?

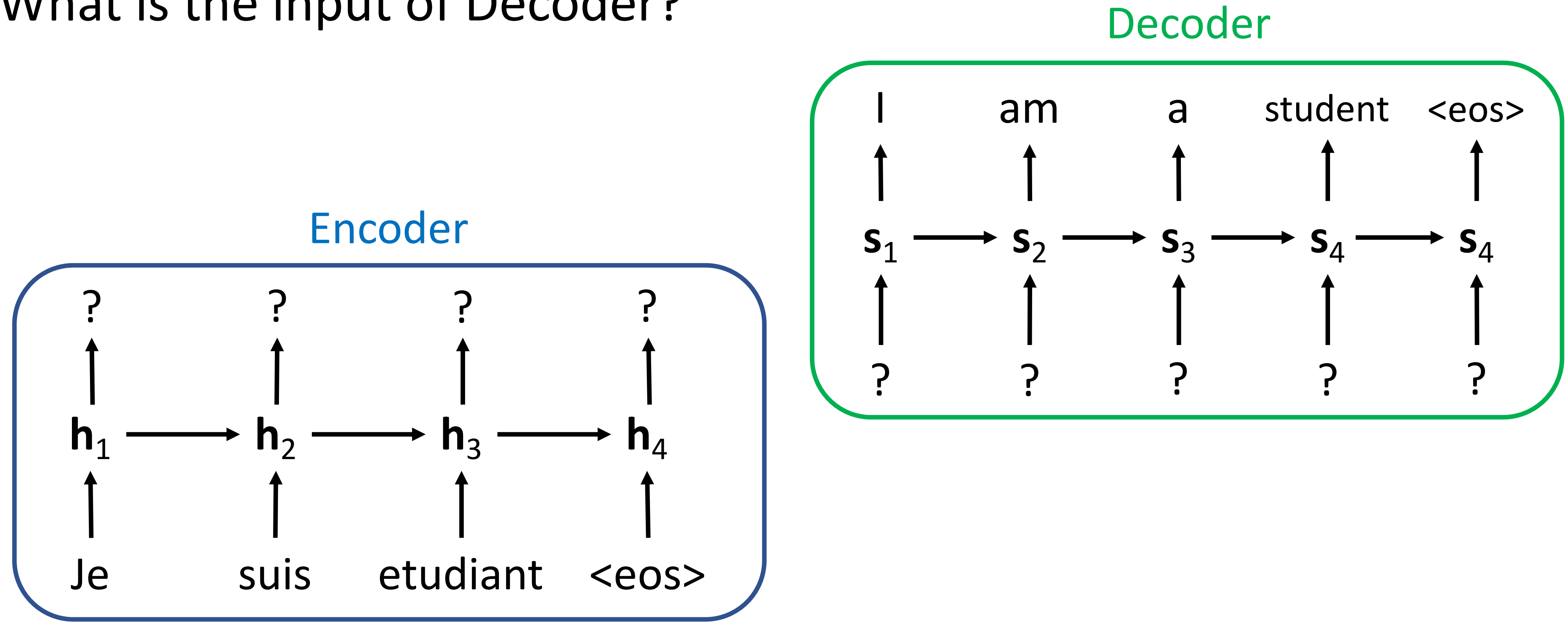
Machine Translation

- "Je suis etudiant" ➔ "I am a student"
  - French-to-English



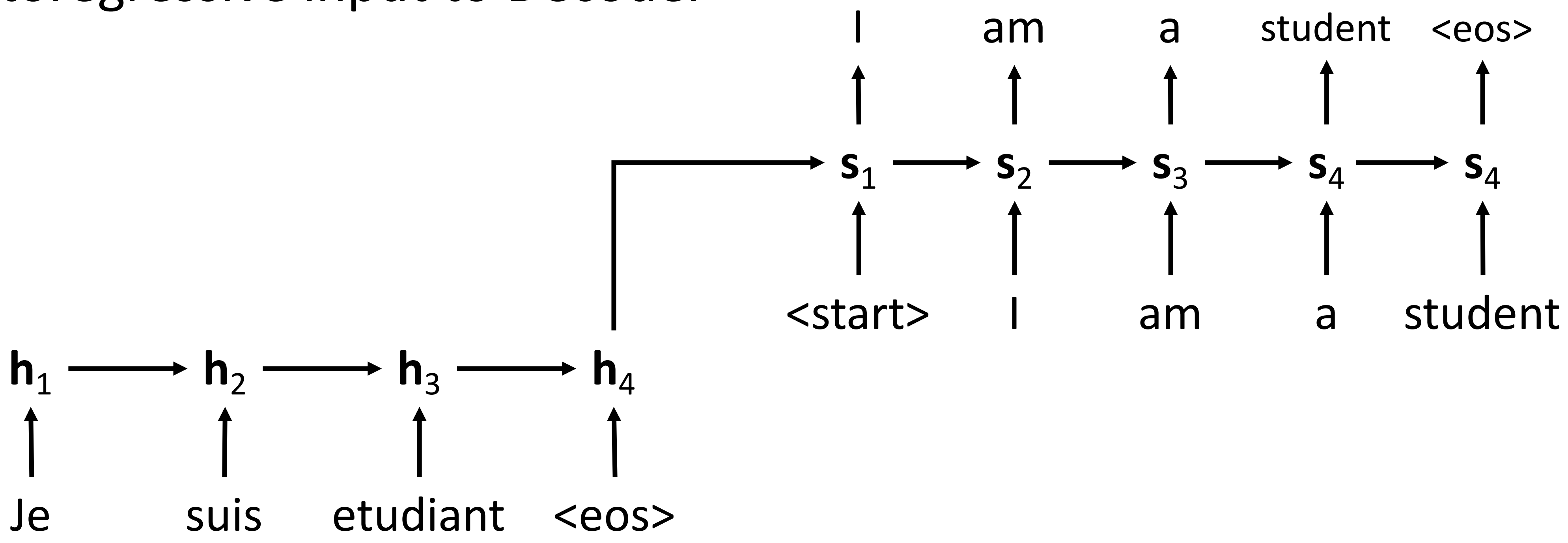
Machine Translation

- What is the output of Encoder?
- What is the input of Decoder?



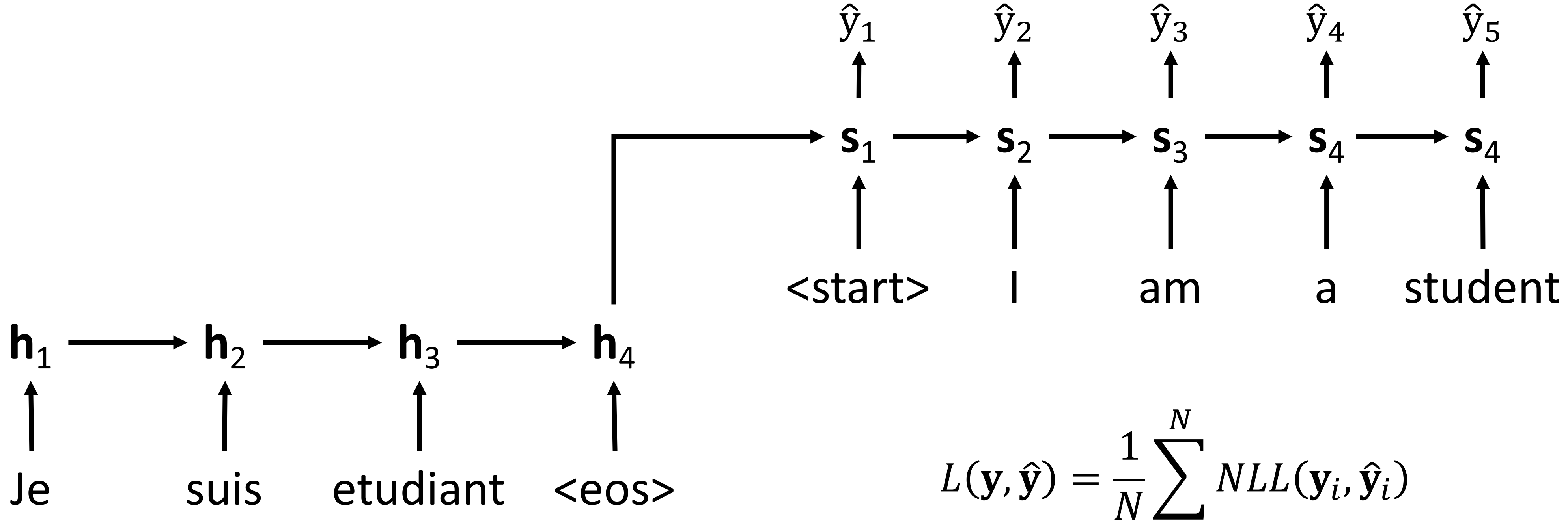
Machine Translation

- Encoder's last hidden layer is the initial state of Decoder
  - $\mathbf{h}_4$ represents the input sentence
- Autoregressive input to Decoder



Machine Translation

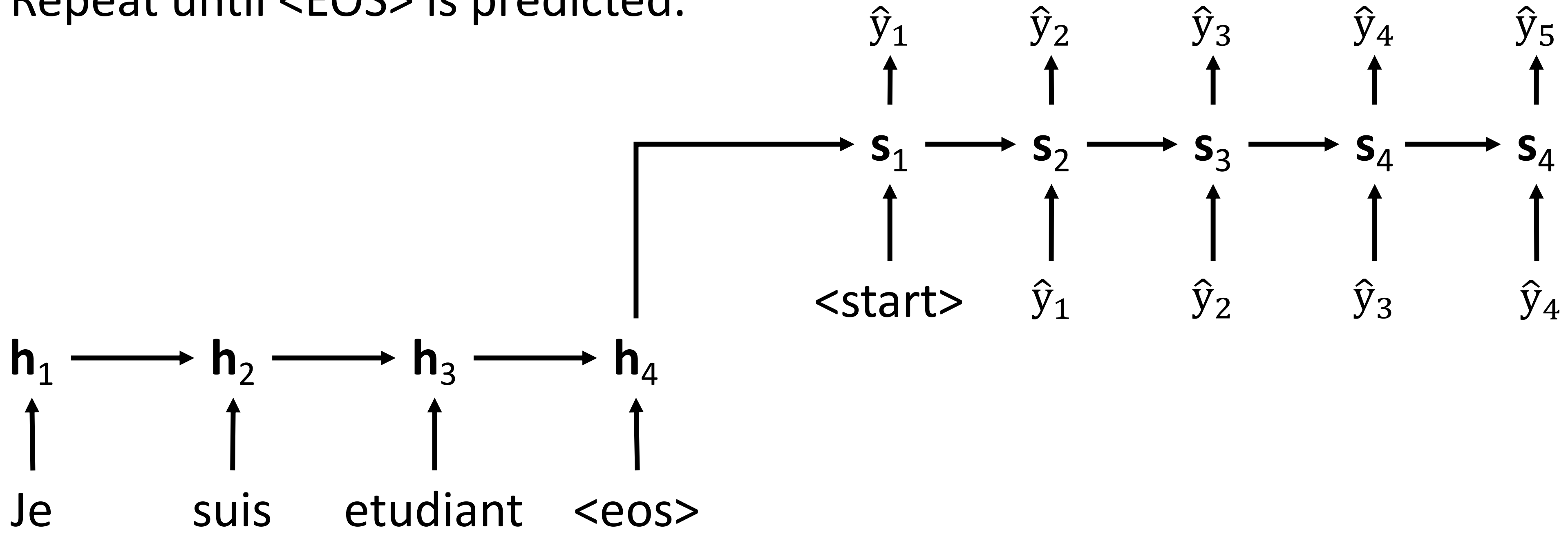
- At training phase:
  - Decoder input is the ground true tokens.
  - Apply negative log-likelihood to predicted outputs.



$$L(\mathbf{y}, \hat{\mathbf{y}}) = \frac{1}{N} \sum_{i=1}^{N} NLL(\mathbf{y}_i, \hat{\mathbf{y}}_i)$$

Machine Translation

- At test phase:
  - Decode input is the previous predicted token.
    - Autoregressive input
  - Repeat until <EOS> is predicted.



Attention

Attention models

- Bahdanau, Cho, Bengio, 2014
  - English-French translation using RNN
- Let's use hidden layers from all timesteps to make predictions

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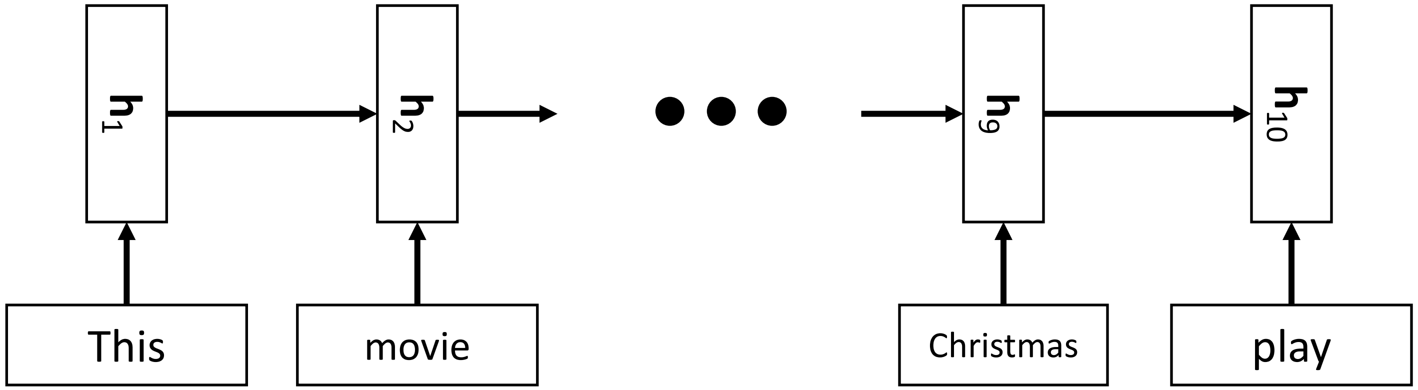

Attention models

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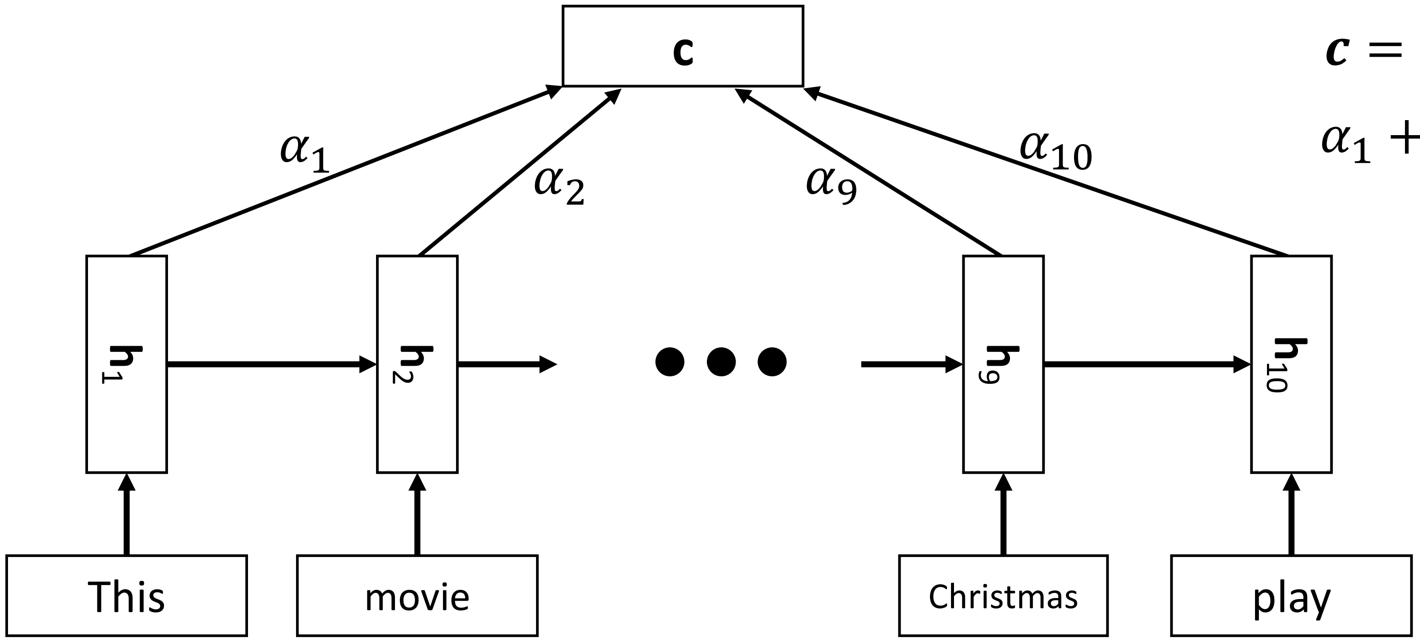
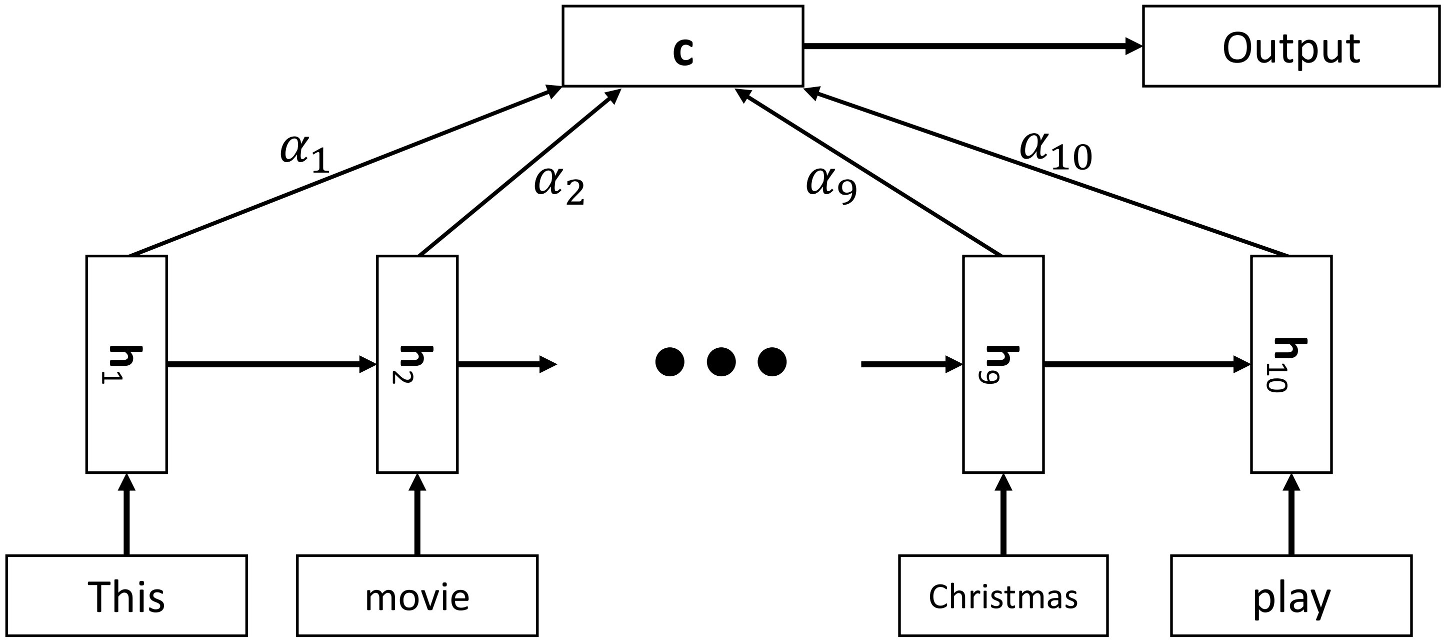


$$\boldsymbol{c} = \alpha_1 \boldsymbol{h}_1 + \alpha_2 \boldsymbol{h}_2 + \cdots + \alpha_{10} \boldsymbol{h}_{10}$$

$$\alpha_1 + \alpha_2 + \cdots + \alpha_{10} = 1$$

Attention models

- Bahdanau, Cho, Bengio, 2014
  - English-French translation using RNN
- Let's use hidden layers from all timesteps to make predictions



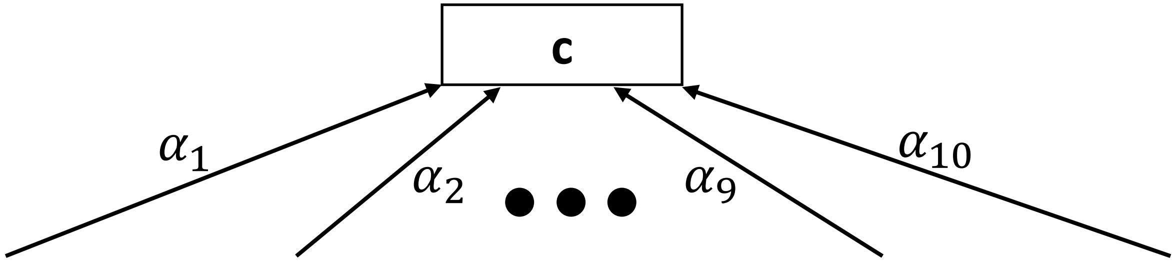
y = $\boldsymbol{\sigma}(\mathbf{w_o}^{T}\mathbf{c})$

Attention models

- Attention, what is it good for besides improved performance?

Attention models

- Attention, what is it good for besides improved performance?



- Now **c** is an explicit combination of all past information
  - $\alpha_1, \alpha_2, \cdots, \alpha_{10}$ denote the usefulness from each word
  - We can tell which word was used the most/least to the outcome
- Attentions α_i are generated using an MLP

How to generate the attentions α_i?

- Use another feedforward neural network model

Output y $\quad y = \mathbf{w_o}^T \mathbf{h}$ (outcome $-\infty \sim +\infty$)

Hidden Layer **h** $\quad \mathbf{h} = \boldsymbol{\sigma}(\mathbf{W_h}^T \mathbf{x})$

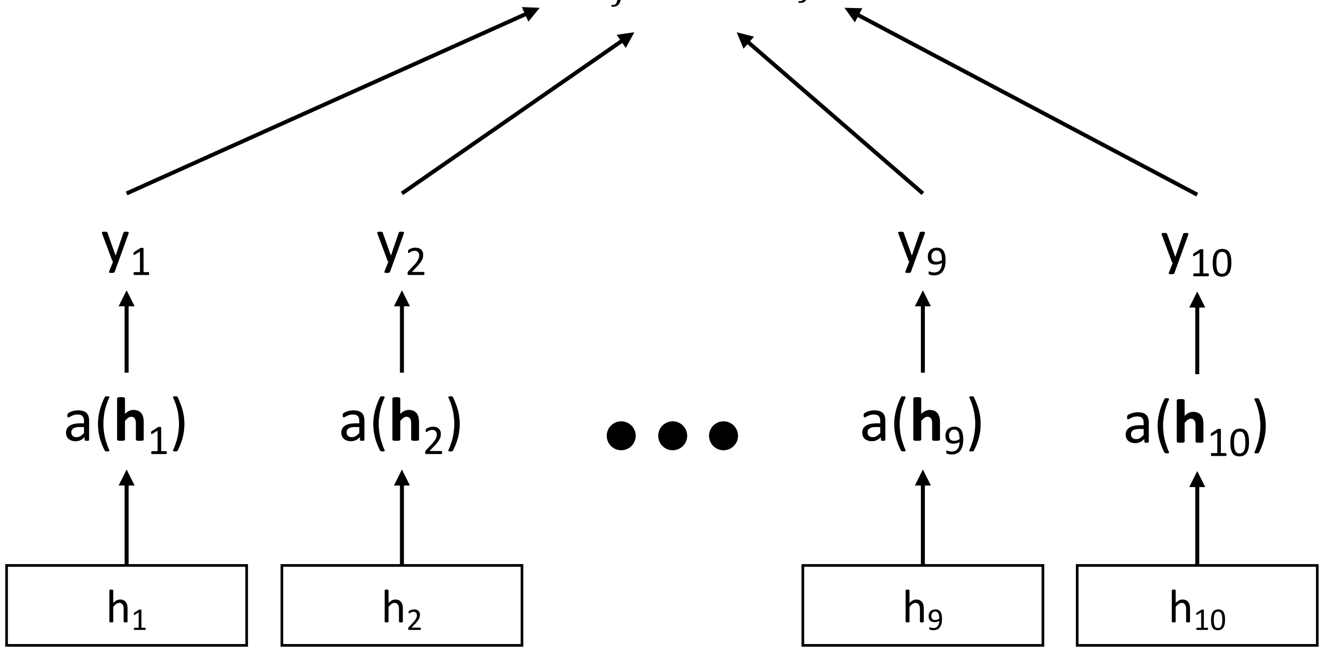
Input Layer **x** $\quad \mathbf{x}$

Let's call this function y=a(**x**)

How to generate the attentions α_i?

- Use function a(.) for each $\mathbf{h}_i$
  - Feed the scores y_1, y_2, …, y_{10} into the Softmax function

$$\alpha_i = \frac{\exp(y_i)}{\sum_{j=1}^{10} \exp(y_j)}$$

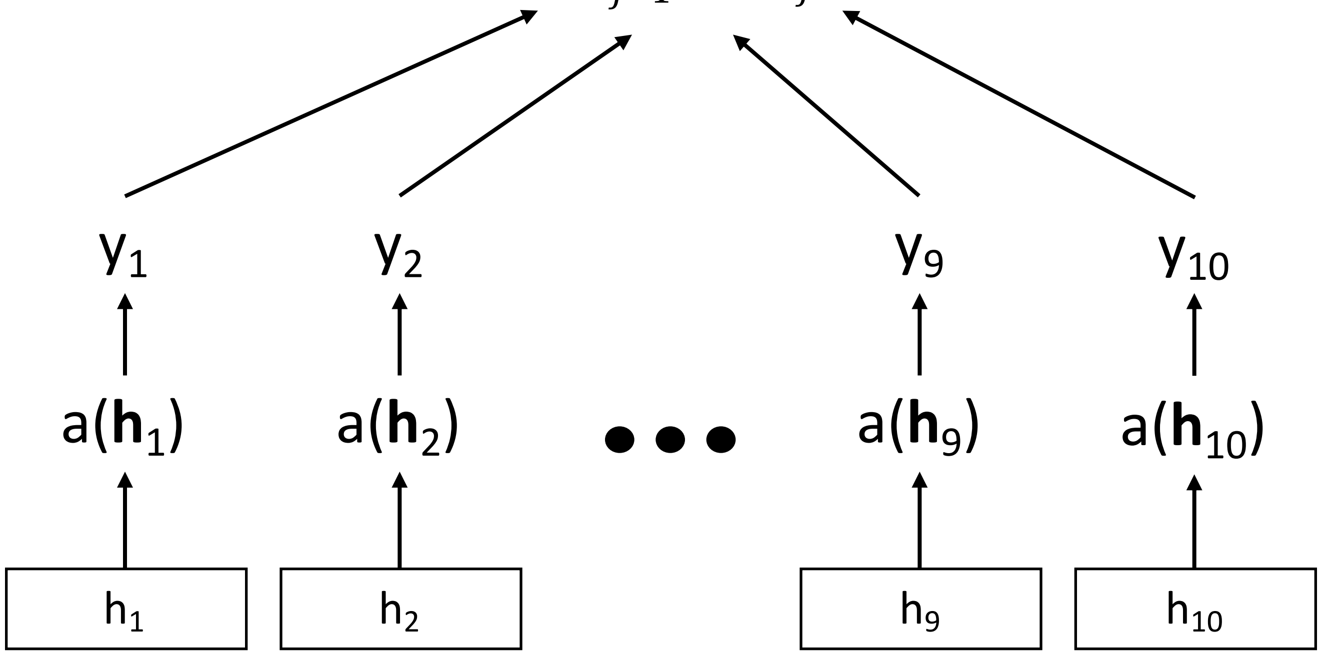


How to generate the attentions α_i?

- Use function a(**x**) for each word: Justice, League, …, Christmas, play
  - Feed the scores y_1, y_2, …, y_{10} into the Softmax function

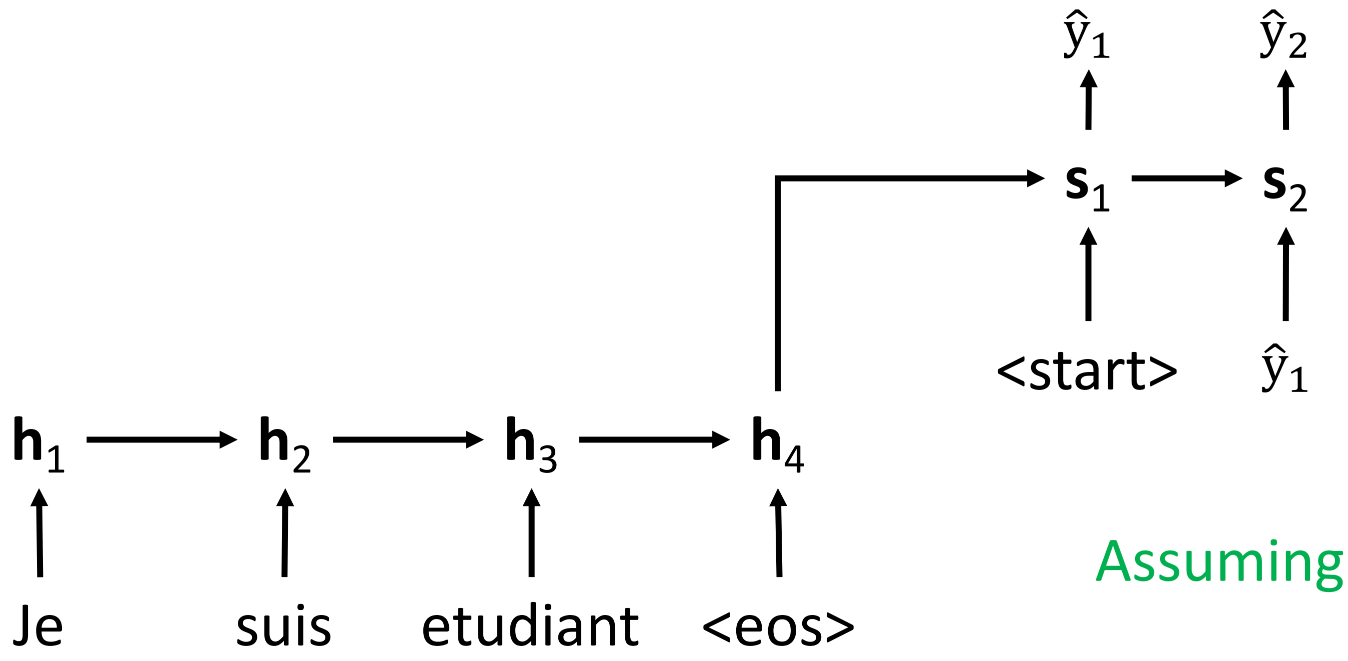
$$\alpha_i = \frac{\exp(y_i)}{\sum_{j=1}^{10} \exp(y_j)}$$

Softmax function ensures α_i's sum to 1



Attention in Seq2Seq

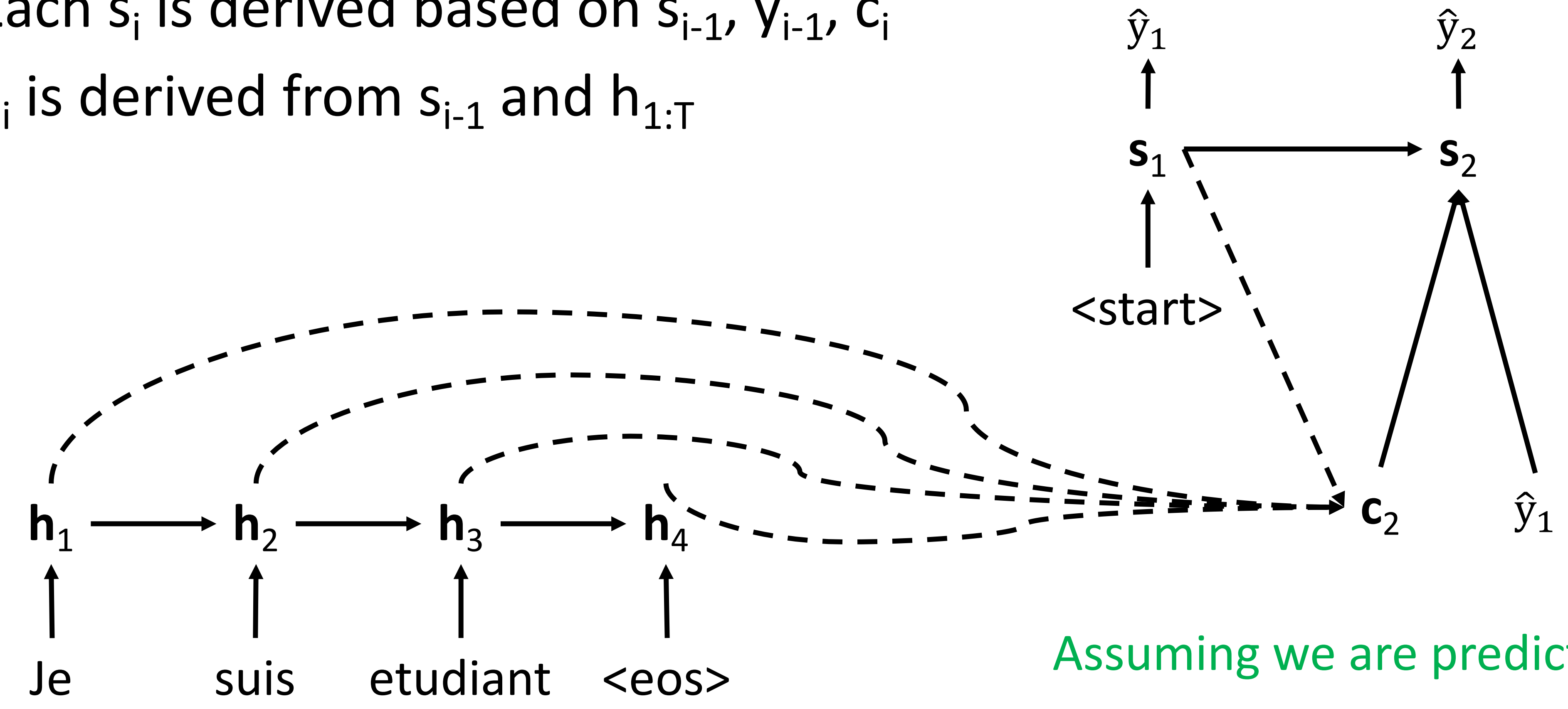
- Each y_i is predicted based on s_i
- Each s_i is derived based on s_{i-1}, y_{i-1}



Assuming we are predicting y_2

Attention in Seq2Seq

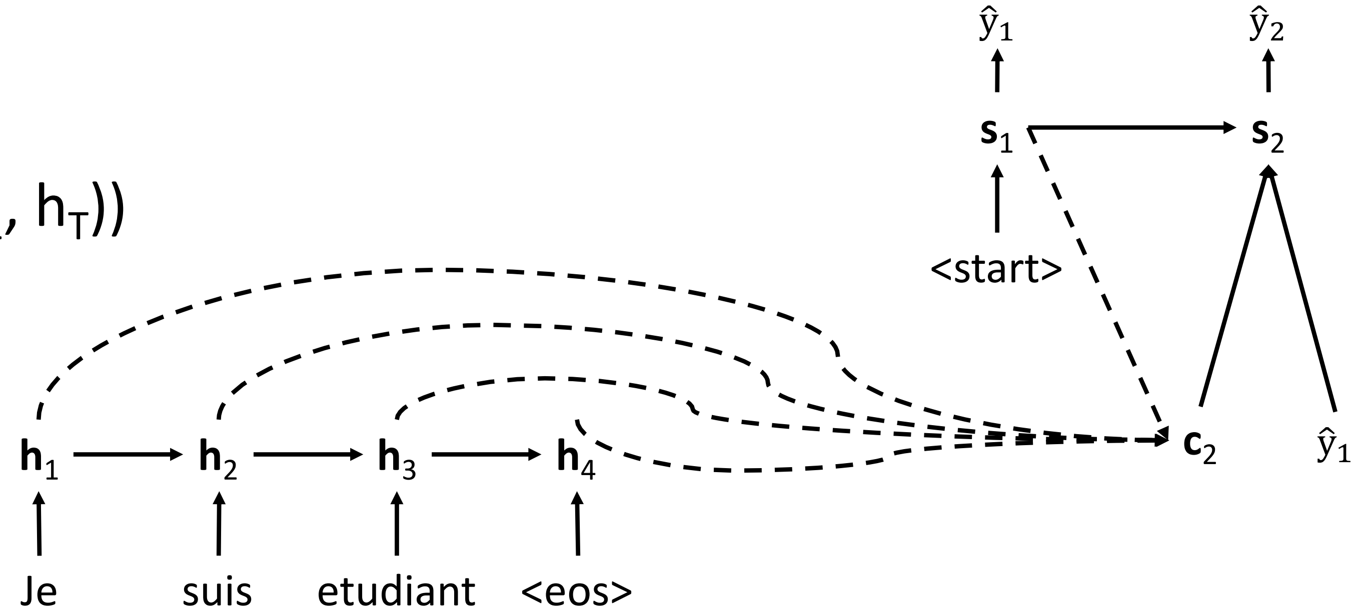
- Each y_i is predicted based on s_i
- Each s_i is derived based on s_{i-1}, y_{i-1}, c_i
- c_i is derived from s_{i-1} and $h_{1:T}$



Assuming we are predicting y_2

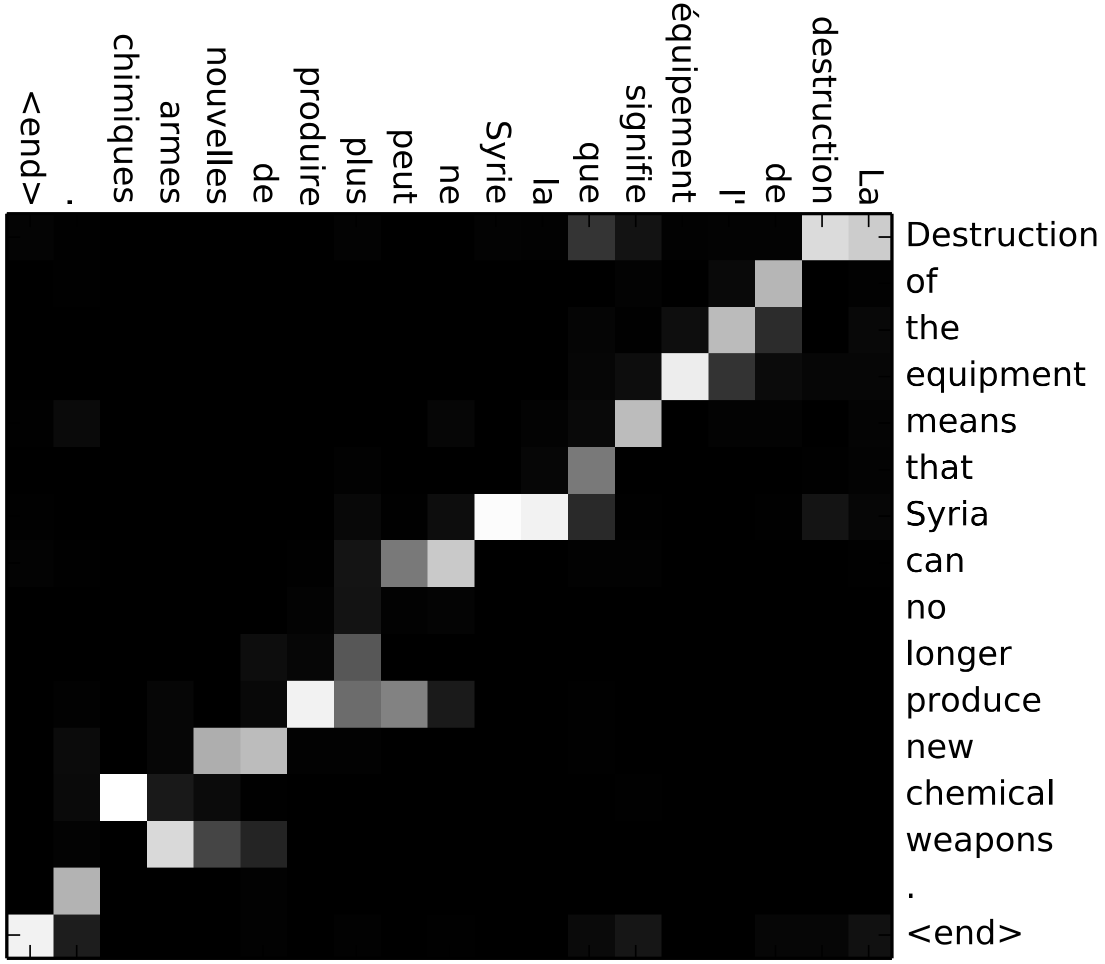
Attention in Seq2Seq

- Each y_i is predicted based on s_i
  - y_i = Softmax($W_w s_i$ + b)
- Each s_i is derived based on s_{i-1}, y_{i-1}, c_i
  - s_i = RNN(s_{i-1}, $[y_{i-1};c_i]_{concat}$)
- c_i is derived from s_{i-1} and $h_{1:T}$
  - c_i = sum(α_i*h_i)
  - α_i = Softmax(f(s_{i-1}, h_1), … , f(s_{i-1}, h_T))
  - f(s_{i-1}, h_j) = $s_{i-1}^T W_f h_j$



Attention Example

- English-French translation
  - Bahdanau, Cho, Bengio 2014



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